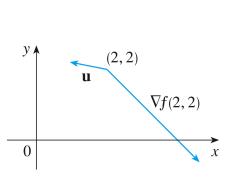
Lesson 17. Maximizing the Directional Derivative

0 Warm up

Example 1. Use the figure below to estimate $D_{\vec{u}}f(2,2)$. Assume $|\nabla f(2,2)| \approx 3$, and the angle between $\nabla f(2,2)$ and \vec{u} is approximately $3\pi/4$.

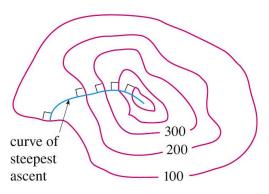


1 Maximizing the directional derivative

• From the previous lesson: in words, the directional derivative of f at (x, y) in the direction of unit vector \vec{u} is

• Questions:

- In which direction does *f* change the fastest? (steepest ascent or descent)
- What is this maximum rate of change?
- Important theorem: (f is a function of 2 or 3 variables)
 - $\circ~$ The maximum value of $D_{\vec{u}}f$ is $|\nabla f|$
 - $\circ~$ The maximum value occurs when \vec{u} is in the $\underline{\text{same}}$ direction as ∇f



• As a result, the gradient is

2	Examples
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Example 2. Let $f(x, y) = xe^y$. a. Find the rate of change of f at the point P(2,0) in the direction from P to $Q(\frac{1}{2},2)$. b. In what direction does f have the maximum rate of change? What is this maximum rate of change? **Example 3.** Find the directional derivative of $f(x, y) = \sqrt{xy}$ at P(2, 8) in the direction of Q(5, 4).

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